

fca.sty

L^AT_EX-macros for Formal Concept Analysis

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Abstract

Formal Concept Analysis is a mathematical field based on the theory of lattices and ordered sets, with applications in data analysis and knowledge processing. To simplify typesetting of FCA-related text, `fca.sty` provides two environments and some simple macros, just for convenience. `fca.sty` offers nothing that you could not do without. The two environments are `cxt` for typesetting small formal contexts as cross-tables, and

`diagram` for making line diagrams of concept lattices. This environment may be of some interest for other purposes as well, since it can also be used for ordered sets and graphs.

A recent version of `fca.sty` should be available from

www.math.tu-dresden.de/~ganter

1 Environment `cxt`

What this (very simple) environment does can be guessed from an example: The text on the left leads to the output on the right.

```
\begin{cxt}%  
\cxtName{Formula 1}%  
\att{1.}%  
\att{2.}%  
\atr{disqualified}%  
\obj{x.}{Alonso}  
\obj{.x.}{Schumacher}  
\obj{.xx}{Montoya}  
\end{cxt}
```

Formula 1	1.	2.	disqualified
Alonso	×		
Schumacher		×	
Montoya		×	×

`cxt` generates a tabular of the appropriate format. The tabular is defined as soon as the first `\obj` command is given. Spaces in the lines before are not ignored (in this version). Therefore, each line should be ended with a `%`. (To be repaired in later versions).

The commands within a `cxt`-environment are

`\cxtName{}` Define the text for the upper left cell of the table. Optional. The default is no text.

`\att{}` Give an attribute name. These names are processed in the order in which they are given. Attribute names given after an `\obj` command are ignored.

`\atr{}` Same as `\att{}`, but with rotated text.

`\obj{v}{}` Give an object's name and its incidence vector, consisting of dots and 'x's. The incidences come first, for better alignment. The length of each incidence vector must be the number of attributes.

Each instance of `\obj` is directly translated to a row of the `tabular`-environment. It is therefore possible to mix `\obj` commands with usual `tabular`-commands.

`cxt` can handle up to 20 attributes.

The arrow relations may also be used. Instead of `x` and `.`, type `d` (for "down"), `u` ("up"), or `b` ("both"), as in the following example:

```

\begin{cxt}%
\renewcommand{\cxtArrowStyle}{\footnotesize\color{red}}
\cxtName{Formula 1}%
\att{1.}%
\att{2.}%
\atr{disqualified}%
\obj{xbd}{Alonso}
\obj{uxb}{Schumacher}
\obj{bxx}{Montoya}
\end{cxt}

```

Formula 1	1.	2.	disqualified
Alonso	×	↗	↗
Schumacher	↗	×	↗
Montoya	↗	×	×

The default for `\cxtArrowStyle` is `\footnotesize`. In the above example we have changed it using `\renewcommand` in order to make the arrows red. The default colour is black.

2 Environment diagram

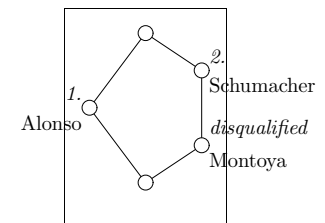
The `diagram` environment helps typesetting diagrams of concept lattices, but can be used for ordered sets and graphs as well. Again we start with a small example (for which we have set `\unitlength 1.2mm`):

```
\begin{diagram}{40}{55}
\node{1}{20}{10}
\node{2}{35}{20}
\node{3}{5}{30}
\node{4}{35}{40}
\node{5}{20}{50}
\edge{1}{2}
\edge{1}{3}
\edge{2}{4}
\edge{3}{5}
\edge{4}{5}
%\Numbers
\leftAttbox{3}{2}{2}{1.}
\rightAttbox{2}{2}{2}{disqualified}
\rightAttbox{4}{2}{2}{2.}
\leftObjbox{3}{2}{2}{Alonso}
\rightObjbox{2}{2}{2}{Montoya}
\rightObjbox{4}{2}{2}{Schumacher}
\end{diagram}
```



Here are the commands of the `diagram`-environment:

```
\begin{diagram}{width}{height} translates to
\begin{picture}(width,height)(\diagramXoffset,\diagramYoffset).
The offsets are zero by default. They can be modified using \renewcommand.
Note that the diagram dimensions do not take the labels into account, these
may overlap. Putting an \fbox around the above diagram yields (with
\unitlength .7mm)
```

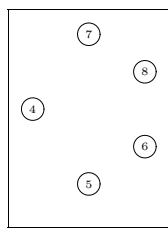


`\Node{nodenumber}{xpos}{ypos}` Puts a circle at position (xpos,ypos) of the picture. These circles are drawn when `\end{diagram}` is invoked. The default diameter of the circles is 4 (times `\unitlength`). It can be changed (for all circles) with `\CircleSize{}`. The node numbers must be different, consecutive between 0 and 51, but need not necessarily be given in ascending order.

The present version of `diagram` does not support blackened or colored circles.

`\Numbers` Puts numbers inside circles. While working on a diagram it can be helpful to have a picture with numbered nodes. The result of the following command sequence is shown on the right:

```
\fbox{\unitlength .7mm
\begin{diagram}{40}{55}
\node{5}{20}{10}
\node{6}{35}{20}
\node{4}{5}{30}
\node{8}{35}{40}
\node{7}{20}{50}
\numbers
\end{diagram}}
```



We recommend to remove the `\Numbers`-command when the diagram is ready. In most cases it is not a good idea to put text inside the nodes of a diagram.

`\Edge{nodenumber1}{nodenumber2}` Puts a line between the two nodes with the given numbers. These must have been declared earlier with a `\Node`-command. For nodes with coordinates (u,v) and (x,y) the command translates to

`\drawline(u,v)(x,y).`

The `\Edge`-command is executed immediately. It can be mixed with other `picture`- and `epic`-commands like `\spline`. Line thickness can be set with `\thicklines`, `\Thicklines`, `\thinlines`, and `\allinethickness{}` (see the `epic` manual).

`\leftAttbox{nodenumber}{xoffset}{yoffset}{text1\ \ text2\ \ ...}`

This is one of six commands

`{\left, \center, \right} \times {Attbox, Objbox}.`

`\NDDArrow` Gives $\not\Leftarrow$ the symbol for the negation of \Leftarrow .

`\NDDPfeil` Same as `\NDDArrow`.

`\Semi` Gives $\bar{\times}$, the symbol for the semi-product.

`\FCA` Prints “Formal Concept Analysis”. In most cases, this command does not eat the space following it (thanks to `\xspace`).

`\FBA`, `\FnBA` Print “Formale(n) Begriffsanalyse”. These commands also use `\xspace` so that blanks are preserved.

Some symbols that are provided by \LaTeX are listed in Figure 2.

Here is a sample text:

`\FCA` offers an elegant way to determine the congruence relations of a complete lattice: The congruence lattice of a doubly founded concept lattice \mathcal{CLGMI} is isomorphic to $\mathcal{CL}(G,M,\not\Leftarrow)$.

This translates to:

Formal Concept Analysis offers an elegant way to determine the congruence relations of a complete lattice: The congruence lattice of a doubly founded concept lattice $\mathfrak{B}(G, M, I)$ is isomorphic to $\mathfrak{B}(G, M, \not\Leftarrow)$.

4 To do

- Allow shaded and half-shaded nodes in diagrams, and make them (optionally) automatic for object- and attribute concepts.
- Improve the code to avoid unwanted blanks.

`\context[S]` Other letters, such as \mathbb{S} , may also be used.

`\CL` The symbol $\underline{\mathfrak{B}}$ for the concept lattice operator. If \mathbb{K} is a formal context, then $\underline{\mathfrak{B}}(\mathbb{K})$ denotes its concept lattice.

`\BV` same as `\CL`.

`\CLGMI` The concept lattice $\underline{\mathfrak{B}}(G, M, I)$ of the formal context (G, M, I) .

`\BVGMI` Same as `\CLGMI`.

`\CGMI` The set $\mathfrak{B}(G, M, I)$ of all formal concepts of the formal context (G, M, I) .

`\BGMI` Same as `\CGMI`.

`\extent` The extent $\text{ext}(\mathfrak{c})$ of the formal concept $\mathfrak{c} := (A, B)$ is A .

`\intent` The intent $\text{int}(\mathfrak{c})$ of the formal concept $\mathfrak{c} := (A, B)$ is B .

`\extents` The set $\text{Ext}(\mathbb{K})$ of extents of the formal context \mathbb{K} .

`\intents` The set $\text{Int}(\mathbb{K})$ of intents of the formal context \mathbb{K} .

`\HNI` The subcontext $(H, N, I \cap H \times N)$.

`\reII` The incidence relation I .

`\notI` The negation \bar{I} of the incidence relation.

`\bigtimes` The product symbol \times .

`\DownArrow` The \swarrow of the arrow relations.

`\Runterpfeil` Same as `\DownArrow`.

`\UpArrow` The \nearrow of the arrow relations.

`\Hochpfeil` Same as `\UpArrow`.

`\DoubleArrow` The $\rlap{\swarrow}\nearrow$ of the arrow relations.

`\Doppelpfeil` Same as `\DoubleArrow`.

`\IUpArrow` Gives \nwarrow , which is has the same meaning as \nearrow , but is drawn in the other direction. This is needed in the definition of $\swarrow\swarrow$.

`\IHochpfeil` Same as `\IUpArrow`.

`\DDArrow` Gives $\swarrow\swarrow$, the symbol for the transitive closure of the arrow relations.

`\DDPfeil` Same as `\DDArrow`.

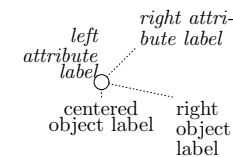
These are used to put text to diagram nodes. The `Attbox`-commands place the text above the corresponding node, the `Objbox` below. Similarly, the text can be placed to the left, be centered, or be placed to the right of the labelled node. All this can be modified with the `xoffset`, `yoffset`-parameters.

The offsets increase the placement effect. A `\rightObjbox`, which is placed to the lower right of the corresponding node, will be moved even further to the lower right if the offsets are positive. Similarly, positive offsets will push a `\leftAttbox` even more to the upper left, etc.

The text of the label is put in a `\parbox`. It can be broken into several lines using `\`. The width of the `\parbox` is `\LabelBoxWidth`, with a default value of 40mm. This can be changed using `\renewcommand`.

The label text and the labelled node are connected with a dotted line. Here is an example:

```
{\unitlength .7mm
\begin{diagram}{40}{15}
\Node{0}{20}{10}
\leftAttbox{0}{1}{1}{left\
attribute\
label}
\rightAttbox{0}{10}{10}{right
attri-\
bute label}
\rightObjbox{0}{20}{5}{right\
object\
label}
\centerObjbox{0}{0}{5}{centered\
object label}
\end{diagram}}
```



The style of the labels is given by

```
\ObjectLabelStyle      Default: \small\baselineskip6pt\rm
\AttributeLabelStyle   Default: \small\baselineskip6pt\it.
```

These values can be changed with `\renewcommand`.

`\end{diagram}` This concludes the diagram. The circles representing the nodes are drawn and filled with white. Everything inside such a circle (except for the numbers caused by the `\Numbers` command) is erased.

Package error messages for the `diagram` environment are not yet implemented. Errors usually are caused by using node numbers that have not been defined earlier.

2.1 Problems with pdfL^AT_EX

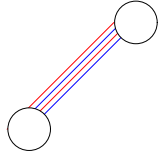
The `diagram` environment uses `eepic.sty`, which is not supported by pdfL^AT_EX. When used with pdfL^AT_EX, `fca.sty` loads `eepicemu.sty` as a substitute. But the result are unsatisfactory. To obtain good pdf output, we recommend to use L^AT_EX, then `dvips` and `ps2pdf`.

Older versions of `fca.sty` used a variable `ifpdf` that caused problems with recent settings of TeL^AT_EX: it forced pdfL^AT_EX. This has been repaired.

2.2 Problems with colour

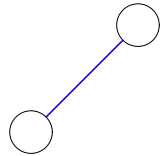
Since the diagrams are drawn using the `picture`-commands and the `eepic` package, we can combine with other packages, for example, with the `color` package. This allows us to colour edges and text, but not nodes. However, `color` has a problem with spacing. Changing colors can cause unwanted spaces, and these are particularly unpleasant in pictures. Have a look at the following:

```
{\unitlength 2mm
\begin{diagram}{20}{20}
\node{1}{5}{5}
\node{2}{15}{15}
{\color{red}\Edge{1}{2}}
{\color{blue}\Edge{1}{2}}
{\color{red}\Edge{1}{2}}
{\color{blue}\Edge{1}{2}}
\end{diagram}}
```



This effect disappears when spaces are avoided. Here is a better version:

```
{\unitlength 2mm
\begin{diagram}{20}{20}
\node{1}{5}{5}
\node{2}{15}{15}
{\color{red}\Edge{1}{2}}%
{\color{blue}\Edge{1}{2}}%
{\color{red}\Edge{1}{2}}%
{\color{blue}\Edge{1}{2}}%
\end{diagram}}
```



3 Some macros

For a short description see Figure 1.

`\GMI` The formal context (G, M, I) .

`\context` The symbol \mathbb{K} , a frequently used name for a formal context.

Result	command	German version
(G, M, I)	<code>\GMI</code>	
\mathbb{K}	<code>\context</code>	
\mathbb{L}	<code>\context[L]</code>	
\mathfrak{B}	<code>\CL</code>	<code>\BV</code>
$\mathfrak{B}(G, M, I)$	<code>\CLGMI</code>	<code>\BVGMI</code>
$\mathfrak{B}(G, M, I)$	<code>\CGMI</code>	<code>\BGMI</code>
<code>ext()</code>	<code>\extent{}</code>	
<code>int()</code>	<code>\intent{}</code>	
<code>Ext()</code>	<code>\extents{}</code>	
<code>Int()</code>	<code>\intents{}</code>	
$(H, N, I \cap H \times N)$	<code>\HNI</code>	
I	<code>\relI</code>	
$\not I$	<code>\notI</code>	
\times	<code>\bigtimes</code>	
\bowtie	<code>\Semi</code>	
\downarrow	<code>\DownArrow</code>	<code>\Runterpfeil</code>
\uparrow	<code>\UpArrow</code>	<code>\Hochpfeil</code>
\longleftrightarrow	<code>\DoubleArrow</code>	<code>\Doppelpfeil</code>
\Uparrow	<code>\IUpArrow</code>	<code>\IHochpfeil</code>
\Downarrow	<code>\DDArrow</code>	<code>\DDPfeil</code>
\Nrightarrow	<code>\NDDArrow</code>	<code>\NDDPfeil</code>
Formal Concept Analysis	<code>\FCA</code>	
Formale Begriffsanalyse		<code>\FBA</code>
Formalen Begriffsanalyse		<code>\FnBA</code>

Figure 1: Table of `fca.sty`-macros.

Symbol	command	package required
\vee	<code>\vee</code>	
\wedge	<code>\wedge</code>	
\bigvee	<code>\bigvee</code>	
\bigwedge	<code>\bigwedge</code>	
\sqcup	<code>\sqcup</code>	
\sqcap	<code>\sqcap</code>	
\bigsqcup	<code>\bigsqcup</code>	
\bigsqcap	<code>\bigsqcap</code>	<code>stmaryrd</code>

Figure 2: Other symbols that are used in Formal Concept Analysis, and the commands that generate them.